A Sub-µW Tuneable Switched-Capacitor Amplifier-Filter for Neural Recording using a Class-C Inverter

A. Ghorbani-Nejad* and A. Jannesari* (C.A.)

Abstract: A two stage sub-µW Inverter-based switched-capacitor amplifier-filter is presented which is capable of amplifying both spikes and Local Field Potentials (LFP) signals. Here we employ a switched capacitor technique for frequency tuning and reducing of 1/f noise of two stages. The reduction of power consumption is very necessary for neural recording devices; however, in Switched Capacitor (SC) circuits OTA is a major building block that consumes most of the power. Therefore an OTA-less technique utilizing a class-C inverter is employed that significantly reduces the power consumption. A detailed analysis of noise performance for the inverter-based SC circuits is presented. A mathematical model useful for analysis of such SC integrators is derived and a good agreement has been obtained between simulation and analytical results. With a supply voltage of 0.7V and using 0.18 µm CMOS technology, this design can achieve a power consumption of about 538 nW. The designed amplifier-filter has the gains 18.6 dB and 28.2 dB for low pass only and cascaded filter, respectively. By applying different sampling frequencies, the filter attains a reconfigurable bandwidth.

Keywords: Amplifier-Filter, Inverter-Based Switched-Capacitor Circuit, Neural Recording, Noise Analysis.

1 Introduction
Recent studies in brain-machine interfaces has showed that using local field potentials (LFPs) is necessary especially when chronically implanted microelectrodes functionality decays for recording unit-spikes activity [1]. Multi-channel microprobes have the capability of recording both spike trains and LFPs. Spike signals have bandwidths of 200 Hz to 5 KHz and amplitude levels up to ±500 µV, while LFPs bandwidth is 10 Hz to 100 Hz and their amplitudes reach up to ±5mV [2]. Because of their different characteristics it is difficult to have a stand-alone, small-scale system for simultaneously record them. For the simultaneous recording of both neural signals, the amplifier must have a high dynamic range, which can be limited by the noise performance of an ADC [3].

For recording this signals, a new architecture that uses a two-stage amplifier structure as shown in Fig. 1, has been introduced in [3].

The first stage is a low-pass SC biquad filter with the amplification of 10 times for LFPs and the second stage is a band-pass SC biquad filter with an additional amplification of 10 times for spikes recording. Each stage bandwidth is reconfigurable by using different sampling clock frequencies. To reduce the 1/f noise it uses the chopper modulation at high frequencies. In their design, operational transconductance amplifier (OTA) is used as an active feedback element in the SC biquad filters.

However, OTA consumes most of the power in SC circuits, and it is difficult to design low-voltage and low-power OTAs in scaled CMOS technologies [4, 5]. This paper uses the architecture shown in Fig. 1, but instead of OTA a class-C inverter is applied which enables the design of low-voltage and low-power filters. With this technique the power consumption can be reduced by about 120 times less than that of [3].

Fig. 1 The proposed system architecture for neural recording in [3].
The inverters first used in SC circuits by [6, 7] and because of their attractive properties for designing low-voltage and low-power circuits, again attract attentions [8-11]. The effect of non-idealities such as finite DC-gain and parasitic is considered for the delta-sigma (ΔΣ) modulators [4]. Although the intrinsic noise of inverters has discussed, but a detailed analysis of entire noise in an inverter-based SC integrator (which is an important block in many SC circuits) does not exist. This paper presents a detailed analysis of entire noise in an inverter-based SC integrator due to both switches and inverter intrinsic noise. In addition, this paper also provides design guidelines to minimize noise in an inverter-based SC integrator. A mathematical model useful for analysis of such integrators is derived and a good comparison is obtained between simulation and analytical technique.

Principle operation of SC circuits that uses a class-C inverter instead of OTA is explored in section 2 and a detailed analysis of noise is presented in section 3. In section 4 the design procedure of the circuit is explained. The simulation results are presented in section 5, and finally the section 6 provides the conclusion.

2 Operation of Inverter-Based SC Circuits

2.1 Inverter-Based SC Integrators

Fig. 2 illustrates a typical SC integrator that uses an OTA as an active element to perform a negative feedback. It has two non-overlapping phase clocks: sampling (φ1) and integrating phase (φ2). In sampling phase, input signal (vI) is sampled to sampling capacitor (Cs) and during the φ2 phase the charge is transferred from Cs to integrating capacitor (Ci). Due to the feedback configuration, the node VG forms a virtual ground.

Instead of using an OTA, a simple logic inverter can be used as an active element in SC circuits. In [4] a structure for inverter-based SC integrator was proposed that uses an auto-zeroing technique to form a virtual ground, as shown in Fig. 3(a). During the sampling phase φ1, the offset voltage of inverter (Voff) is sampled in CC. In the φ2 phase, due to the negative feedback, VX should be equal to Voff; therefore VG can form a virtual ground.

Fig. 3(b) shows the pseudo-differential inverter-based SC integrator, with Common Mode Feedback (CMFB), proposed in [4]. During the φ1 phase, the CMFB capacitors (CM) are discharged and during the φ2 phase they form a common mode feedback loop whose gain is defined by CM/Ci ratio. In the design of differential Low-Pass-Filter (LPF) and Band-Pass-Filter (BPF) biquads we use this architecture that will be explained more in Section 4.

2.2 Class-C Inverters

According to the applied supply voltage, the push-pull inverters are classified into class-AB and class-C inverters. If the supply voltage (VDD) is chosen so as to VDD > VTN + VTP in which VTN and VTP are the threshold voltages of NMOS and PMOS transistors, respectively, the inverter behaves as a class-AB amplifier. In this case, the static short circuit current is much more than that of class-C inverters in which VDD < VTN + VTP. Class-C inverters have much more DC-gain than class-AB inverters; however, the gain-bandwidth product of class-AB inverters is much better [4]. The class-C inverter is a suitable case for low voltage and low power design especially in the above mentioned application, where the signal frequencies are not so high. We use class-C inverters in SC LPF and BPF biquads that will be described in section 4.
3 Noise Analysis

3.1 Inverter Intrinsic Noise

The Power Spectral Density (PSD) of the thermal noise current in an MOS transistor can be expressed [12-14] as:

\[ S_{ni,therm}(f) = 4kT \cdot g_m \left[ \frac{A^2}{Hz} \right] \]  

(1)

where is 2/3 and 1/2 for transistors operating in saturation and weak inversion mode, respectively. Assuming, for the simple class-c inverter shown in Fig. 4(a), both transistors have the same trans-conductance \( g_m \). The equivalent PSD of thermal current noise \( S_{ni,eq}(f) \) is the sum of NMOS and PMOS current noise PSDs, i.e. \( S_{ni,N}(f) \) and \( S_{ni,P}(f) \) (Fig. 4(b)).

\[ S_{ni,eq}(f) = S_{ni,N}(f) + S_{ni,P}(f) = 4kT \cdot g_m \left[ \frac{A^2}{Hz} \right] \]  

(2)

Therefore, the input-referred voltage PSD noise of the inverter, denoted by \( S_{nv,eq}(f) \) (Fig. 4(c)), is thus

\[ S_{nv,eq}(f) = \frac{kT}{g_m} \left[ \frac{V^2}{Hz} \right]. \]  

(3)

It is noteworthy to mention the flicker noise has much lower effect than thermal noise due to aliasing of thermal noise and the used auto-zeroing technique, cancels out the low frequency flicker noise [14].

3.2 Analysis of Noise in an Inverter-Based SC Integrator

Analysis of entire noise in an inverter-based SC integrator requires both sampling (\( \phi_s \)) and integrating (\( \phi_i \)) phases to consider. In addition, there are two different noise sources in each phase: inverter intrinsic noise and on-resistance thermal noise of switches.

3.2.1 Integrating Phase

Fig. 5 shows the equivalent circuit of the integrator under integrating phase. \( R_{out} \) denotes the output resistance of inverter and the \( C_I \) accounts both the parasitic and the next stage capacitans.

a) Effect of Inverter Intrinsic Noise

Firstly, we analyze the effect of inverter intrinsic noise at the integrator output while neglecting the on-resistance of two switches \( S_4 \) and \( S_5 \).

It is evident that \( V_1 \) is equal to the voltage division of \( V_{n,eq} \) across \( C_S \) and \( C_I \) plus \( V_{n,eq} \) (i.e. \( V_1 = V_{n,eq} + V_{out} \left[ C_I / (C_I + C_S) \right] \)). Applying the KCL at the output node and assuming large enough \( R_{out} \), the transfer function \( H(s) \) can be derived as:

\[ H_1(s) = \frac{V_{n,eq}(s)}{V_{n,eq}(s)} = 1 + s \left( \frac{C_{out} \cdot G_0}{2 \cdot g_m} \right) \]  

(4)

where the DC gain \( G_0 = 1 + \frac{C_S}{C_I} \) and the output capacitance \( C_{out} = C_L + \frac{C_I \cdot C_S}{C_I + C_S} \).

Therefore, the total integrated noise power can be expressed as:

\[ V_{n,eq}^2 \left( \frac{2}{kT} \right) \int_0^\infty \frac{V_{n,eq}^2(f) \cdot H_1(j2\pi f)^2}{df} = \frac{kT \cdot G_0}{2 \cdot C_{out}}. \]  

(5)

Eq. (5) indicates that increasing \( C_s \) and \( C_I \) so that the ratio of them (also \( G_0 \)) remains unchanged, cause the lower output-referred noise due to the intrinsic inverter noise.

b) Effect of On-Resistance Thermal Noise of Switches

The two switches that appear ON in this phase (i.e. \( S_4 \) and \( S_5 \)) are modeled as \( R_{on4} \) and \( R_{on5} \). Each one generates a white noise PSD equal to \( 4kTR_{on} \) (Fig. 5). Since, the noise sources are uncorrelated, the transfer function from each one to the output can be find separately to find the contribution of each one on the entire output noise power. Hereafter, it is assumed both switches have the same \( R_{on} \) for simplicity.

The Transfer functions from \( V_{n,S_S} \) and \( V_{n,S_5} \) approximately can be expressed as Eq. (6) and Eq. (7), respectively.

\[ H_{05}(s) = 1 + s \left( \frac{C_{out} \cdot G_0}{2 \cdot g_m} \right) \]  

(6)

\[ H_{04}(s) = 1 + s \left( \frac{C_{out} \cdot G_0}{2 \cdot g_m} \right) \]  

(7)

![Fig. 4 A simple inverter with (a) device nosies, (b) equivalent output-referred current and (c) equivalent input-referred voltage noise sources.](image)

![Fig. 5 Equivalent circuit of the integrator under integrating phase.](image)
\[
H_2(s) = \frac{V_{\text{out}}(s)}{V_{n,S_5}} \approx \frac{1}{1 + 2C_L \left( \frac{C_j + C_S}{C_j C_S} + 4RonC_L\right)} \quad (6)
\]

\[
H_3(s) = \frac{V_{\text{out}}(s)}{V_{n,S_4}} \approx \frac{1}{C_L/C_S + \left( RonC_L + \frac{C_j + C_L}{2gm} \right)s} \quad (7)
\]

Thus, the total integrated noise power at the output due to each one is given by:

\[
\begin{align*}
\frac{V_{\text{out}}}{n_{out}^2} &= \int_0^\infty \left[H_2(j2\pi f)\right]^2 df \\
&= \frac{kT}{4CL} \frac{1}{\left( \frac{C_j + C_S}{C_j C_S} \right)} \quad (8)
\end{align*}
\]

\[
\begin{align*}
\frac{V_{\text{out}}}{n_{out}^2} &= \int_0^\infty \left[H_3(j2\pi f)\right]^2 df \\
&= \frac{kT}{C_I^2} \frac{C_SR_{on}}{R_{on} + \frac{1}{2gm} \left( \frac{C_j + C_L}{C_j} \right)} \quad (9)
\end{align*}
\]

From Eq. (9), it can be noted that the effect of \( V_{n,S_4} \) on the output can be neglected if \( g_mR_{on} \gg 1 \).

### 3.2.2 Sampling Phase

**a) Effect of Intrinsic Inverter Noise**

The equivalent circuit under sampling phase (\( \phi \)) is shown in Fig. 6(a). Under assumption that the switches have very low on-resistance, the transfer function from inverter intrinsic noise to the output can be expressed the same as (4) whereas \( C_I \rightarrow \infty \), (Fig. 6(b)).

Therefore, the total integrated output noise power due to inverter intrinsic noise, can be derived as:

\[
\frac{V_{\text{out}}}{n_{out}^2} = \frac{kT}{2(C_L + C)} \quad (10)
\]

It is clear that increasing the \( C_L \) can be reduced the effect of inverter intrinsic noise on the total output noise.

**b) Effect of On-Resistance Thermal Noise of Switches**

In this case, the three switches \( S_1, S_2 \), and \( S_3 \) become ON and have contribution on integrator overall noise performance.

Fig. 6(c) shows the equivalent circuit for deriving the effect of \( S_1 \), thermal noise in which \( Z_1 \) denotes the parallel impedance looking into the circuit. Practically, \( Ron_1 \) is too small so that \( Z_1 \) has no effect. Thus, the total integrated noise appeared across \( C_L \) can be written as:

\[
\frac{V_{\text{out}}}{n_{CS}^2} = \frac{kT}{2C_S} \quad (11)
\]

The transfer function from output to \( V_{n,S_2} \) has a complicated expression that cannot be solved easily. However for having some useful insight for designing purpose, several simplification has made and finally it can be approximated as

\[
H_5(s) = \frac{V_{\text{out}}(s)}{V_{n,S_2}} \approx \frac{1}{1 + \frac{C_L}{C_C} + 4gmRon + 2RonC_Ls} \quad (12)
\]

Therefore, the approximated total integrated output noise power due to \( V_{n,S_2} \) will be

\[
\frac{V_{\text{out}}}{n_{out}^2} \approx \int_0^\infty \left[H_5(j2\pi f)\right]^2 df \\
= \frac{kT}{2C_L} \frac{1}{\left( \frac{C_L}{C_C} + 4gmRon \right)} \quad (13)
\]

Using the approximated transfer function (14) the total integrated noise power due to the thermal noise of switch \( S_3 \) can be written as Eq. (15).

\[
H_6(s) = \frac{V_{\text{out}}(s)}{V_{n,S_3}} \approx \frac{1}{1 + \frac{C_L}{C_C} + 2RonC_Ls} \quad (14)
\]

\[
\frac{V_{\text{out}}}{n_{out}^2} \approx \int_0^\infty \left[H_6(j2\pi f)\right]^2 df = \frac{kT}{2C_L} \frac{1}{\left( \frac{C_L}{C_C} \right)} \quad (15)
\]

![Fig. 6](attachment://fig6.png)

Fig. 6 (a) Equivalent circuit of the integrator under sampling phase in addition to various noise sources. (b) The simplified circuit for analyzing the effect of inverter intrinsic noise and (c) the equivalent circuit for deriving the effect of \( S_1 \) on-resistance thermal noise on the entire noise behavior.
Form both Eqs. (13) and (15) it can be found that, increasing the $C_L/C_C$ ratio (if it is possible) can be reduced the effect of $V_{n,S_2}$ and $V_{n,S_3}$ on the total output noise power.

### 3.2.3 The Overall Noise Model

Fig. 7 shows the overall noise model for the inverter-based SC integrator. It consists of two noise sources, the total noise power on $s_C$ which is obtained by Eq. (11) and $V_{no,eq}$ denotes the sum of all integrated noise powers given as follows.

$$V_{no,eq}^2 = V_{n,out_1}^2 + V_{n,out_2}^2 + V_{n,out_3}^2 + V_{n,out_4}^2 + V_{n,out_5}^2 + V_{n,out_6}^2$$

(16)

Thus, from this model the total output-referred noise PSD can be obtained as:

$$S_{total}(f) = S_{n,C_S}(f)|H(z)|^2 + S_{no,eq}(f)$$

(17)

where $H(z)$ is the transfer function of the integrator.

Since both noise sources in the model Fig. 7 are sampled with sampling frequency $f_s$, the PSDs in Eq. (17) should computed as $S_{n} = 2V_{n}^2/f_s$ in which $V_{n}$ can be both $V_{n,C_S}$ and $V_{no,eq}$.

Finally, integrating $S_{out}$ over the entire bandwidth gives the total output-referred noise Eq. (18).

$$V_{n,out}^2 = \int_0^\infty S_{total}(f) df$$

(18)

### 4 Circuit Design Procedures

#### 4.1 Switched Capacitor Low Pass Filter

In order to realize a low pass filter stage, a second-order biquad SC circuit was chosen. Fig. 8 illustrate a fully differential SC low pass stage as a Chebyshev type-I filter which uses class-C inverters instead of OTA. The inverters’ power supply and simulated DC-gain are 0.7 V and 32.9 dB, respectively, while their static current is only 77.3 nA. The switched capacitors have two non-overlapping clocks $\phi_1$ and $\phi_2$. The transfer function of this filter can be written as:

$$H(s) = \frac{-80f_s^2}{s^2 + f_s s + 8f_s^2}$$

(19)

where $f_s$ is the sampling frequency. By applying different sampling frequencies, it is clear that the filter can be made tunable.

The low pass stage plays two different roles. When we are interested in LFP signals, it is a low pass filter with about 80Hz bandwidth and 1 KSamples/sec sampling frequency. However, when the system wants to record spikes, this stage works as a gain stage with bandwidth of about 8 KHz and 100 KSamples/sec sampling frequency.

#### 4.2 Switched-Capacitor Band-Pass Filter

To allow spikes only and to prevent the low-frequency signals, a band-pass filter is applied for the second stage. Similar to the low-pass stage, the band pass stage is a fully differential second-order inverter-based biquad SC circuit, as shown in Fig. 9. The transfer function of this stage is given as follows:

$$H(s) = \frac{-2.5f_s s}{s^2 + \frac{1}{4}f_s s + \frac{1}{50}f_s^2}$$

(20)

### Table 1 The Capacitor Values Used in Simulation.

<table>
<thead>
<tr>
<th>Capacitor</th>
<th>$C_S$</th>
<th>$C_L$</th>
<th>$C_C$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Value (fF)</td>
<td>500</td>
<td>250</td>
<td>100</td>
</tr>
</tbody>
</table>

Fig. 8 Differential inverter-based SC low pass implementation.
Fig. 9 Differential inverter-based SC band pass implementation.

where $f_s$ is the sampling frequency. With 100 KSample/sec sampling frequency, the filter has about 4.5 KHz bandwidth whose the center frequency is 1.8 KHz. By applying different sampling frequencies the cut-off frequencies can be made reconfigurable.

4.3 Half-Clock Delay

In order to cascade two stages, a half- delay clock stage is needed to break the continuous loop and to reduce the loading effect of the stages. Thus a simple stage such as one introduced in [9] (shown in Fig. 10) is located between output and input lines of LPF and BPF stages.

4.4 Clock Bootstrapping

When the supply voltage is reduced the switch on-resistance increases, thus in order to have an adequately low switch resistance in low voltage era, the clock voltage should be bootstrapped beyond the supply voltage range. For this reason we use the clock boosted driver in [15] as illustrated in Fig. 11.

5 Simulation Results

For evaluating the performance of the proposed circuits, simulations were performed in Cadence Spectre. The circuit was designed with 0.18-µm CMOS technology. With a 0.7 V supply voltage, the system consumes only 538 nW power (excluding clock generation) which is very suitable for neural recording application. A class-C inverter having 32.9 dB DC-gain and 77.3 nA static current is used in both stages.

The transfer function of low pass stage for 1 KSamples/sec sampling frequency is illustrated in Fig. 12(a). The low pass cut-off frequency is 90 Hz with a DC gain of 18.6 dB which senses the LFP signals. Fig. 12(b) shows the transfer function of the low pass stage for sampling frequency of 100 KSamples/sec. In this case this stage is only a gain stage for spike signals. It demonstrates 8.4 KHz cut-off frequency and 17.8 dB DC gain. Fig. 13 illustrates the simulated cascaded stage, transfer function with 100 KSamples/sec sampling frequency.

The pass band is in the range between 680 Hz and 5 KHz and the center frequency is located at 1.8 KHz with the pass band gain 28.2 dB.

Using PNOISE tool in Cadence Spectre, the total integrated input referred noise of the system, computed as 6.42 µV/√Hz with 8.4 KHz noise bandwidth. This can be translating as 70.1 nV/√Hz input noise density with 8.4 KHz noise bandwidth.

Fig. 14 shows the frequency response of the system for three different supply voltages. As shown, it is not very sensitive to the variation of the supply voltage showing that the design is robust and could be a good choice for neural recording systems.

Table 2 summarizes the specification of some recently published neural amplifiers. The presented structure has quite good power consumption. But in comparison to other works, it has a good noise performance.

6 Conclusions

The large number of channels in multichannel microprobes and, the implantation of the system in the body, necessitate a low power design for neural recording applications. It has been shown that the OTA-less inverter-based technique greatly satisfies this requirement so that a sub-µW system which is composed of two stages has been designed. Using switched capacitor technique enables the adjustable cut-off frequency of the system by applying different sampling frequencies, so that both LFP and spike signals could be filtered and amplified. Also, a detailed analysis of noise performance for the inverter-based SC circuits has been presented. A mathematical model useful for analysis of such SC integrators has been derived and a good comparison between simulation and analytical technique has been obtained.

Fig. 10 A simple half-clock delay stage [8].

Fig. 11 Boosted clock driver [15].
Table 2 Performance Comparison

<table>
<thead>
<tr>
<th>Specification</th>
<th>[16]</th>
<th>[17]</th>
<th>[18]</th>
<th>[19]</th>
<th>[3]</th>
<th>This work¹</th>
</tr>
</thead>
<tbody>
<tr>
<td>Supply voltage (V)</td>
<td>1.8–3.3</td>
<td>1.8</td>
<td>3</td>
<td>1</td>
<td>1.6</td>
<td>0.7</td>
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<tr>
<td>Power/channel (µW)</td>
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<td>15</td>
<td>3.77</td>
<td>69</td>
<td>0.538</td>
<td></td>
</tr>
<tr>
<td>Gain (dB)</td>
<td>41/50.5</td>
<td>59.5</td>
<td>48–68</td>
<td>45.7/49.3/53.7/60.5</td>
<td>19.1/37.5</td>
<td>18.6/28.2</td>
</tr>
<tr>
<td>High-pass corner (Hz)</td>
<td>0.05/0.4/2.5</td>
<td>10–100</td>
<td>0.01–70</td>
<td>0.23–217</td>
<td>100–660</td>
<td>680</td>
</tr>
<tr>
<td>Low-pass corner (Hz)</td>
<td>180</td>
<td>9.1k</td>
<td>500–5k</td>
<td>7.8k</td>
<td>80–8k</td>
<td>90–8.4k</td>
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<tr>
<td>Input referred noise (µVrms)</td>
<td>0.95</td>
<td>8</td>
<td>7</td>
<td>4.43</td>
<td>2.36</td>
<td>6.42</td>
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<tr>
<td>Input-noise density (nV/√Hz)</td>
<td>95</td>
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<td>99</td>
<td>40.4</td>
<td>26.4</td>
<td>70.1</td>
</tr>
<tr>
<td>Technology (µm)</td>
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<td>0.5</td>
<td>0.35</td>
<td>0.35</td>
<td>0.18</td>
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</table>

¹Although this may not a fair comparison, this results are simulated results, whereas the others are measured ones.

References


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