Wavelet Based Automatic Phase Picking Algorithm for 3-Component Broadband Seismological Data

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ABSTRACT: A phase picking algorithm has been developed for P-wave arrival detection and picking on a 3-component broadband seismogram. The algorithm is based on Wavelet Transform, Akaike Information Criteria (AIC) picker and voting mechanism. The mathematical functions have been used to cut up data into different frequency components and each component with a resolution matched to its scale is studied. Continuous Wavelet Transform (CWT) has been applied to pre-filtered 3-component broadband seismograms to compute scales of interest. Wavelet coefficients have been calculated in a sliding time window and AIC picker is applied to these coefficients. Consistency of 3 components picks is the primary criteria of phase detection. Further, for phase picking, AIC picker is applied on the filtered seismogram in the same time window where phase is detected. The comparison of the present algorithm has been checked with the time domain automatic phase pickers and manual picks by seismologists. The algorithm has been tested on regional earthquake data acquired through deployment of broadband seismological station in Garhwal Kumaon Himalayan region and shows a good agreement between analyst picks and auto picks.

Keywords: Phase picking algorithm; P-wave detection; 3-component broadband data

1. Introduction

Seismic data collection is a prerequisite for the disaster mitigation and by introducing digital seismic data acquisition, the long term continuous recording and archiving of seismic signals has became a demanding technical problem. A seismic network or even a single station operating continuously at high sampling frequency produces an enormous amount of data, which is often difficult to store (and analyze) locally or even at the recording center of a network. It is of paramount importance to devise automatic trigger algorithms, which automatically picks the first P-wave arrival so that only the data on events is collected and the information is available online. Automatic phase picking here means detecting and picking accurately the first P-wave arrival, as quickly as possible. It is immensely helpful for finding event location and its identification for source mechanism analysis. Phase picking is also helpful in systems, which releases alert messages quickly after an earthquake. Such warning systems are dependent on automatic, quasi real-time procedures for detecting and onset picking in seismogram recordings. Automatic methods are needed for such picking as manual picking is time consuming and subjective.

Automatic phase picking algorithm remains one of the current research topics and a number of different methods have been implemented in the past to detect and pick seismic phases and estimate their onset time, from single-component as well as three component (3-C) recordings. Most of the event detectors and phase pickers are based on the
the filtered seismogram, in the same time window, moving time window, again detection. Once there is detection in the current wavelet coefficients over multiple scales. Consistency irrelevant one (i.e. noise) decay quickly at larger resolutions. Important features (such as phase arrival) signal is then decomposed into different scales, in filters to enhance the signal to noise ratio (SNR). The broad band array is presented. Such wavelet transform has advantages over traditional Fourier methods in analyzing physical situations where the signal contains discontinuities and sharp spikes. Wavelets were developed independently in the fields of mathematics, quantum physics, electrical engineering, and seismic geology/geophysics. The multidisciplinary approaches during the last decades have led to many new wavelet applications such as image compression, turbulence, human vision, radar, and earthquake prediction. Because seismic waves traveling through complex media are composed of time-frequency-localized waveforms, it is a better choice to represent the seismogram locally both in time and frequency domains. Wavelet transform, which was evolved from the work on seismic signal [12-13], is a very powerful tool for the analysis of such non-stationary signals.

Wavelet transform can be accomplished in two ways: Continuous Wavelet Transform (CWT) and Discrete Wavelet Transform (DWT). The CWT is defined as follows.

\[
W(a,b) = \frac{1}{\sqrt{a}} \int_{-\infty}^{\infty} x(t) \psi \left( \frac{t-b}{a} \right) dt
\]

(1)

Where \( g(t) \) is the wavelet function, and \( a \) and \( b \) are the scale and translation factors, respectively. The wavelet function \( g(t) \) decays rapidly to zero with increasing \( t \) and has zero mean. The domain (range) of nonzero values of the wavelet is called the support. The scale factor controls the dilation or compression of the wavelet, whereas at lower scales, the wavelet is compressed and characterizes the rapidly changing details of the signal. At higher scales,
the wavelet is stretched over a greater time span and the slowly changing and coarse features are better resolved [30].

In practical applications, the DWT is generally preferred because waveforms are recorded as discrete time samples. DWT can be implemented quickly via the Mallat algorithm [17-18]. A low-pass filter and high-pass filter can be used to calculate the wavelet coefficients of a discrete time series recursively. The following tree clearly shows how DWT is implemented using recursively half band filters, see Figure (1). Fourier transform gives us the global information of the frequency content available in the signal. Local frequency content cannot be analyzed using Fourier transform. Wavelet transform has advantage over the Fourier transform because of its ability to characterize the signal features locally with a detail matched to its scale.

### Figure 1. The Subband Coding Algorithm.

3. AIC Picker

AIC picker is a mathematical function whose value can be calculated for each sample of a time series. The global minimum value of AIC gives us the optimal separation of time series and this is the feature of AIC picker which is mostly exploited in many ways in various applications. There are two equations available for calculating AIC values viz using Autoregressive coefficients and without using them.

For AR-AIC (Autoregressive-AIC) approach, the seismogram, i.e., the time series is divided into locally stationary segments, each one is modeled as an AR process, and intervals before and after the onset time are two different stationary processes [23]. The AIC is then used to determine the order of AR process when fitting the portion of the seismogram, which indicates the badness and unreliability of the model fit [1]. When the order of AR process is fixed, the AIC function gives us the measure of the model fit. The point where AIC gives a minimum value (in least square sense) is the optimal separation of the two stationary time series [23]. This is known as AR-AIC picker approach [2, 14, 23]. The AIC of the two interval model for seismogram x of length N is represented as function of merging point k [23];

\[
AIC(k) = (k - M) \log(\sigma_1^2_{\text{max}}) + (N - M - K) \log(\sigma_2^2_{\text{max}}) + C_2
\]  

(2)

Where M is the order of an AR process fitting the data, C_2 is a constant, and \(\sigma_1^2_{\text{max}}\) and \(\sigma_2^2_{\text{max}}\) indicate the variance of the seismogram in the two intervals not explained by the autoregressive process.

The second approach of computing the AIC function is without using AR coefficients, which can be calculated directly from the time series, i.e., the seismogram. The onset point is again the minimum of the AIC function. For seismogram x of length N, the AIC value is defined as [16];

\[
AIC(k) = K \log \left\{ \text{var}(x[k+1,N]) \right\} + (N - k - 1) \log \left\{ \text{var}(x[K+1,N]) \right\}
\]  

(3)

where k ranges through all the seismogram samples.

The AIC picker defines the onset point as the global minimum. For this reason, it is necessary to choose a time window that includes only the seismogram segment of interest [30]. In our work, Eq. (3) is used for calculating AIC function. Figure (2) shows the seismic signal in the upper traces and the corresponding AIC values computed from it in the lower traces. For a seismogram with very clear onset, AIC values have a very clear global minimum. Figure (2a), which corresponds to P-wave arrival. For a seismogram with relatively low SNR, there may be several local minima but the global minimum still gives accurately the P-wave onset, see Figure (2b). If SNR is very low, global minimum is not very clear and can not be identified as a phase onset, see Figure (2c). So here lies the shortcoming that our algorithm may not detect phase onset if SNR is low (which is also the problem with other phase picker algorithms). Also for multiple
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Figure 2. Seismograms and their corresponding AIC values. (a) Clear P-wave arrival. (b) Clear P-wave arrival with relatively lower S/N ratio (c) Very low SNR seismogram (d) Multiple phases available in a single window. (e) Random noise, where global minimum is not a phase arrival.

irrespective of its being a phase or noise, see Figure (2e). Therefore there is a need to choose an appropriate time window and instead of looking into the AIC values of data only, we go for calculation of AIC values of seismogram segment over multiple scales.
4. Automatic Phase Picker Development and Testing

The first step in the processing is the filtering of the seismogram. Seismogram is filtered for signal enhancement prior to applying the wavelet AIC picker. For this algorithm, 5 pole Butterworth band pass filter is used to pass 2-10 Hz band. This band is chosen after looking into Short Time Fourier Transform (STFT) of several P-wave arrivals, which lie in this band. Wavelet AIC picker combines the AIC picker with multiscale wavelet analysis, in which the AIC picker is applied to absolute wavelet coefficients at different scales. For P-wave arrival detection, the AIC picker must pick the phase at different scales, within a proximity to each other, see Figure (3a) and Figure (3b). All three components of seismogram and decompose each component are used into 3 scales. After choosing a suitable time window, the AIC values are calculated for all 3 decomposed components and the consistency of picks were considered. This is achieved by voting mechanism such as checking the consistency of each pick with the other as well as counting the number of times the picks was checked. Maximum voting for such consistency check is $36^4C_2$. If the count of votes crosses a pre-decided threshold, a phase is detected in the current time window. Each component is decomposed into 3 scales which is most appropriate [30]. If more scales are used, the COIs of those singularities that are not isolated will have more overlap and cause more ambiguities. If only two scales are used, however, the singularity due to the noise will still be significant at scales 1 and 2 in some cases, resulting in too much false detection [30].

After detection of event, the picking is achieved
by again applying AIC picker to the vertical component of filtered seismogram, in the current time window. This pick is our final P-wave onset. Vertical component is chosen for picking as it has the maximum sensitivity to P-wave arrival.

Main criteria for choosing a wavelet function from a vast family are its support, symmetry, regularity and number of vanishing moments [28]. In our study, Daubechies wavelet of order 2 is used, which is appropriate for detecting signal singularity and has tighter support of 4.

The main objective of using the wavelet transform is to guide the work of the AIC picker by choosing an appropriate time window for it, in which a P-wave arrival exists [30]. The time window is chosen via a trial and error process and we found 12 sec window quite suitable. Smaller time windows may lead to sluggish detection process as there is a need to overlap consecutive windows in order to reduce the border effect. On the other hand, larger windows may include multiple phases and our picker will pick the stronger phase which may not be first P-wave arrival. For decomposing the signal into different scales, CWT was used and for checking the consistency among picks, the proximity of picks within 1 sec (i.e. 100 samples) was checked. If picks in a time window are consistent more than 20 times (i.e. vote count is ≥ 20), out of 36, we consider it as P-wave detection. The AIC picker picks the onset time after applying it on the vertical component of seismogram in current time window.

Our algorithm allows the user to choose any filter combination, wavelet function, percentage overlap of neighboring windows, time duration for consistency check and the length of time window (with a default setting of 2-10 Hz, “db2” wavelet, 20% overlapping, 1 sec and 12 sec respectively). Figures (4a), (4b), (5a) and (5b) gives the examples

![Figure 4](image)

**Figure 4.** (a) Seismogram segment marked with Analyst pick (vertical component). (b) AIC values corresponding to the seismogram in Figure (4a), minima of AIC values clearly shows the consistency.
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This algorithm has been tested on 450 seismograms from different earthquake events recorded on a single station. The parameters i.e. filter band, wavelet function, percentage overlap, length of time window and number of samples for proximity or consistency check, are all optimized to some extent by trial and error method, applying over the different subsets of the main data set again and again with different parameter settings. Figure (6) shows percentage of events picked accurately by this algorithm within 0.5 sec of analysts’ picks, wrong detection (or false alarms), undetected events and later phases detected (i.e. S-phase).

The AIC based picker has also been checked with other available automatic phase pickers. The phase picking was carried out using the STA/LTA base simple phase picker program available with the data processing software, Sharma et al [22] APP in which the filters were incorporated in the time domain while computing the STA and LTA, and the AIC phase picker using the single component i.e., without using voting criteria for three component. The results are summarized in Table (1). In all 450 seismograms which were checked for the four types of algorithms, the AIC picker using 3 component has detected 279 picks within 0.5 seconds, while using...
Table 1. Comparison of the Phase picking algorithm on the data.

<table>
<thead>
<tr>
<th>Sl. No.</th>
<th>Name of the PickerView</th>
<th>Picks with 0.5sec</th>
<th>False Alarms</th>
<th>Undetected Events</th>
<th>Later Picks Detected</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>AIC Picker 3 Comp.</td>
<td>279</td>
<td>103</td>
<td>27</td>
<td>41</td>
</tr>
<tr>
<td>2</td>
<td>AIC Picker Single Comp.</td>
<td>264</td>
<td>115</td>
<td>36</td>
<td>35</td>
</tr>
<tr>
<td>3</td>
<td>Sharma et al [22]</td>
<td>258</td>
<td>121</td>
<td>32</td>
<td>39</td>
</tr>
<tr>
<td>4</td>
<td>STA/LTA</td>
<td>246</td>
<td>136</td>
<td>35</td>
<td>33</td>
</tr>
</tbody>
</table>

The single component program was run on the vertical component only. The horizontal components showed almost similar results. The inclusion of filtering in the computing using Sharma et al [22] criteria of STA and LTA has increased the number of picks by 12. The comparison shows the advantage of the developed 3 component AIC picker.

The 3 component and the single component pickers using AIC have been compared for the picks within 0.5 seconds of the analyst picks in Table (2). The 3 component picker has picked 279 picks while the single component without voting criteria has picked only 264. The comparison shows the increase in accuracy while using the voting criteria.

Table 2. Percentage distribution of all picks picked by the AIC algorithm within 0.5 sec.

<table>
<thead>
<tr>
<th>Sl. No.</th>
<th>With in 0.1sec</th>
<th>0.1 – 0.2sec</th>
<th>0.2 – 0.3sec</th>
<th>0.3 – 0.5sec</th>
<th>0.5sec</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>AIC Picker 3 Comp.</td>
<td>52</td>
<td>21</td>
<td>10</td>
<td>17</td>
</tr>
<tr>
<td>2</td>
<td>AIC Picker Single Comp.</td>
<td>45</td>
<td>20</td>
<td>15</td>
<td>20</td>
</tr>
</tbody>
</table>

5. Conclusions

An algorithm has been developed for automatic P-phase picking using AIC picker combined with multiscale wavelet analysis in the present study. The data acquired through CMG3T broadband seismometer has been used for checking the developed phase picking algorithm. As P-wave arrival in a seismogram is a significant feature therefore it will be retained over several scales, whereas noise or other incoherent features will disappear quickly over larger scales. One of the main advantage of this algorithm over the other algorithm is its checking of the signal in various frequency bands. On the other side, the available phase picking algorithms use the STA/LTA's in one frequency band only. AIC picker is applied directly to the absolute wavelet coefficients calculated from different components of seismogram. Detection criterion is to check consistency quantified as a minimum number, among the picks in different windows (3 components ~9 windows). Picking is achieved by again applying AIC picker to the vertical component of seismogram segment in the current time window. This algorithm has been tested on a dataset of seismic events occurring in the Garhwal Kumaon Himalayan Region. Around 450 events of varying length are checked using these algorithms. The comparison of other such algorithms has shown the advantage of using AIC over the classical phase pickers. The comparison with the manual picks by the analyst shows that using the present phase picker about 62% of auto picks are within 0.5 sec of analyst picks.

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