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Exact Modeling and Simulation of Saturated Induction Motors with Broken Rotor Bars Fault using Winding Function Approach

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ABSTRACT

Winding function method (WFM) provides a detailed and rather simple analytical modeling and simulation technique for analyzing performance of faulty squirrel-cage induction motors (SCIMs). Such analysis is mainly applicable for designing on-line fault diagnosis techniques. In this paper, WFM is extended to include variable degrees of magnetic saturation by applying an appropriate air gap function and novel techniques for estimating required saturation factor and angular position of the air gap flux density. The resultant saturable winding function method (SWFM) is properly applied to analyze SCIMs with broken rotor bars and to identify the saturation effect on the related fault indexes. Comparing simulation results to the corresponding experimental ones show higher accuracy of the SWFM. This means that more precise fault diagnosis techniques can be designed by using the proposed saturable modeling technique.

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NOMENCLATURE

B_{ai}	Air gap flux density next to any rotor mesh i	i_k	Current of the rotor mesh k , $k=1, 2, \dots, R$
B_{cn}	Cosine component of n^{th} space harmonic of the air gap flux density	J	Inertia moment of the rotor and mechanical load
B_{sn}	Sine component of n^{th} space harmonic of the air gap flux density	K_{sat}	Saturation factor
B_n	Amplitude of n^{th} space harmonic of the air gap flux density	l	Stack length
g^{-1}	Inverse air gap function	L_{ii}	Self inductance of the circuit i
g_s	Fictitious air gap function in the presence of saturation	L_{ij}	Mutual inductance between the circuits i and j
g'	Mean value of g_s	l_b	Leakage inductance of the rotor bars
g_0	Effective air gap length of the unsaturated machine	l_e	Leakage inductance of the rotor end ring between two adjacent bars
n_x	Turn function of the x phase (mesh)	i_a, i_b, i_c	Stator phase currents
N_y	Winding function or modified winding function of the y phase (mesh)	Greek Symbols	
P	Number of pole pairs	α_n	Phase angle of the n^{th} space harmonic of the air gap flux density
R	Number of rotor bars (meshes)	α_i	Angle of the center of the rotor bar i
R_s	Resistance of the stator windings	θ_r	Rotor angular position
R_{rb}	Resistance of the rotor bars	φ	Angle in the stator stationary reference frame
R_{re}	Resistance of the rotor end ring between two adjacent bars	φ_f	Angular position of a zero crossing point of the air gap flux density
r	Air gap mean radius	ρ	Peak value of fluctuation of g_s
s	Slip	μ_0	The air magnetic permeability
T_e	Induced torque		

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1. INTRODUCTION

Any factor disturbing electrical, magnetic and/or mechanical symmetry of squirrel cage induction motor (SCIM) can generate undesirable variations of the motor quantities. If these variations are intensified, the motor operation deteriorates or it stops [1-4]. The air gap magnetic flux density is a dominant factor of the motor behavior such that all its quantities including current, torque and power directly depend on this factor [5-11], while in turn; the air gap magnetic flux density is directly affected by the motor core magnetic saturation [9, 12]. Normally, the rotor broken bars in high power electrical motors lead to high local saturation around the breakage part [9]. The local saturation produces backward variations in the air gap flux density and this reflects over all motor variables [1, 13]. On the other hand, precise diagnosis of the fault degree is essential in a proper repair and maintenance process. Meanwhile, use of a precise model, which follows real behavior of the motor with suitable accuracy, can be taken into account as the first stage in the fault diagnosing procedure. Therefore, including the motor core saturation as major factor in the faulty motor behavior is unavoidable [14, 15]. To this end, many attempts have been so far made to deal with this problem; each has its merits and drawbacks.

Application of magnetic harmonic functions is well-known as a procedure for applying core saturation to the motor model [16, 17]. In fact, core saturation is applied analytically to the first and third harmonics of the air gap flux. The advantage of this method is that it does not need to evaluate the inductances considering all harmonics present. In spite of this, efficiency of the model for faulty motor has not been investigated. Magnetic equivalent circuit is another analytical model which is applicable for simulating faulty SCIMs. Core saturation with proper precision has been included in this model and a good agreement between the experimental and simulation results has been achieved [18, 19].

Winding function method (WFM) offers an analytical model widely used to model and simulate the faulty SCIMs due to its rather simple implementation [20-23]. First, linear model has been presented and reluctance variations of the flux path due to the saturation has been ignored [24]. This model has not been recommended to predict the SCIM behavior under the rotor broken bars fault which directly depends on the core saturation level. In spite of this, the linear model has been used for modeling the SCIM with the rotor broken bars fault in different modes, including line-start mode [24] and inverter-fed mode [25]. But, the obtained values of the fault indexes are not applicable because the core saturation has not been applied [13]. In fact, core saturation is the main factor in determining the broken bar fault indexes amplitude [26]. Reference [27] has shown that the difference between the non-saturated and

saturated models regarding fault index amplitudes could be as much as 15 dB.

The first attempt to include core saturation effect in the WFM has been proposed by [28]. The basis of this saturable WFM (SWFM) is application of a saturation factor (K_{sat}) to the linear model and varying the motor inductances in different operating points. The saturation factor has been determined using the air gap voltage fundamental harmonic amplitude, which depends on the rotation speed of the air gap flux density as well as its amplitude, while the saturation degree depends only on the flux density amplitude. To modify the previous SWFM, the method introduced by [29] can be used. However, the broken rotor bars disturb the flux density distribution in the air gap and cause the SWFM introduced [29] to track the air gap flux density incorrectly.

In this paper, modifications are made to the previous SWFM in order to make it applicable to simulate SCIMs with broken rotor bars fault. To do so, the rotor meshes are used as the air gap flux samplers. The flux-linkages of the rotor meshes, which are calculated in every simulation step, are used to estimate the air gap flux density distribution around the air gap. Then, Fourier series analysis is used to determine the space harmonics of the air gap flux density, including fundamental harmonic amplitude (B_1) and its phase angle (α_1). B_1 is used to determine K_{sat} properly and α_1 is utilized to track the air gap flux density. Therefore, a modified version of the SWFM obtains, whose accuracy proves by comparing magnetization characteristics determined through simulation and experiments. Then, using both the modified SWFM and the normal WFM, the performance of SCIM with broken rotor bars is simulated. By comparing the results, impacts of the magnetic saturation on the faulty SCIMs performance and their fault indexes will be clear. Comparisons are also made by experimental results, which confirm the higher accuracy of the proposed SWFM. This means that more precise fault diagnosis techniques can be designed using the proposed saturable modeling technique.

2. SATURABLE WINDING FUNCTION METHOD FOR MODELING SCIMs

In the WFM, any loop on the rotor, consisting of two adjacent rotor bars and portions of the end rings, is considered as a circuit mesh. It means that the rotor includes a number of circuit meshes equal to its slot or bar number. Applying KVL to the rotor meshes and the stator phases and considering related mechanical equations, the dynamic equations for a Δ -connected SCIM can be written as follows [21]:

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$$[V_s] = [R_s][I_s] + \frac{d}{dt}[\psi_s] \quad (1)$$

$$[0] = [R_r][I_r] + \frac{d}{dt}[\psi_r] \quad (2)$$

$$T_e - T_L = J \frac{d\omega}{dt} \quad (3)$$

$$\omega = \frac{d\theta_r}{dt} \quad (4)$$

where:

$$[V_s] = [v_{ab} \ v_{bc} \ v_{ca}]^T \quad (5)$$

$$[I_s] = [i_a \ i_b \ i_c]^T \quad (6)$$

$$[I_r] = [i_1 \ i_2 \ \dots \ i_R]^T \quad (7)$$

$$[\psi_s] = [L_{ss}][I_s] + [L_{sr}][I_r] \quad (8)$$

$$[\psi_r] = [L_{rs}][I_s] + [L_{rr}][I_r] \quad (9)$$

$$T_e = \frac{1}{2}[I_s]^T \frac{\partial [L_{ss}]}{\partial \theta_r}[I_s] + \frac{1}{2}[I_s]^T \frac{\partial [L_{sr}]}{\partial \theta_r}[I_r] + \frac{1}{2}[I_r]^T \frac{\partial [L_{rs}]}{\partial \theta_r}[I_s] + \frac{1}{2}[I_r]^T \frac{\partial [L_{rr}]}{\partial \theta_r}[I_r] \quad (10)$$

$$[R_s] = \begin{bmatrix} R_s & 0 & 0 \\ 0 & R_s & 0 \\ 0 & 0 & R_s \end{bmatrix} \quad (11)$$

$$[R_r] = \begin{bmatrix} 2(R_{rb} + R_{re}) & -R_{rb} & 0 & \dots & -R_{rb} \\ -R_{rb} & 2(R_{rb} + R_{re}) & -R_{rb} & \dots & 0 \\ 0 & -R_{rb} & 2(R_{rb} + R_{re}) & \dots & \vdots \\ \vdots & \vdots & \vdots & \dots & \vdots \\ -R_{rb} & 0 & \dots & \dots & 2(R_{rb} + R_{re}) \end{bmatrix} \quad (12)$$

As seen, various self/mutual inductances of the stator phases and/or the rotor meshes, i.e. elements of the inductance matrices $[L_{ss}]$, $[L_{sr}]$, $[L_{rs}]$ and $[L_{rr}]$, and their derivatives versus the rotor position are the most important parameters within the dynamic equations. Some of these inductances depend on the rotor position. So, by rotating the rotor, they must be updated at each simulation step. According to the winding function or modified winding function theory [22], these inductances are calculated as follows:

$$L_{xy} = \mu_o r l \int_0^{2\pi} g^{-1} n_x N_y d\varphi \quad (13)$$

where x and y represent any phase of the stator (a, b or c) or any mesh of the rotor (1 to R). For uniform air gap machine, N_y is the winding function of the y circuit, but in the case of the non-uniform air gap machine, it is the modified winding function of the y circuit. In the latter case, the modified winding function guarantees the

equality: $L_{xy} = L_{yx}$ for any x and y circuits [22]. Therefore, it can be realized that $[L_{rs}] = [L_{sr}]^T$. A technique to evaluate the impacts of the rotor bars skewing on the elements of the matrix $[L_{sr}]$ has been presented in [21] and used in the simulation procedure. Leakage inductances must be added to the self-inductances and some mutual-inductances obtained from (13) as follows [30]:

$$[L_{ss}] = \begin{bmatrix} L_{aa} + l_{ls} & L_{ab} & L_{ac} \\ L_{ab} & L_{aa} + l_{ls} & L_{bc} \\ L_{ac} & L_{bc} & L_{aa} + l_{ls} \end{bmatrix} \quad (14)$$

$$[L_{rr}] = \begin{bmatrix} L_{11} + 2(l_b + l_e) & L_{12} - l_b & L_{13} & \dots & L_{1R} - l_b \\ L_{21} - l_b & L_{22} + 2(l_b + l_e) & L_{23} - l_b & \dots & L_{2R} \\ L_{31} & \dots & \dots & \dots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ L_{R1} - l_b & L_{R2} & L_{R3} & \dots & L_{RR} + 2(l_b + l_e) \end{bmatrix} \quad (15)$$

Saturation of the magnetic material causes its reluctance to be increased against the machine's flux. Similar increase of the reluctance can be achieved by a proportional increase in the air gap length along the main flux path [14, 28, 29]. Anywhere within the core material, reluctance increases due to the saturation depends on the exact value of the flux density, but independent of the flux direction. Thus, it is expected that the fictitious air gap length fluctuates a complete cycle every half cycle of the flux density distribution around the air gap. Assuming a sinusoidal form for this fluctuation [14], the following relation (16) satisfies the mentioned requirements [29]:

$$g_s(\varphi, \varphi_f, K_{sat}) = g'[1 - \rho \cos(2P(\varphi - \varphi_f))] \quad (16)$$

where g' and ρ are determined as follows:

$$g' = g_0 \frac{3K_{sat}}{K_{sat} + 2} \quad (17)$$

$$\rho = \frac{2(K_{sat} - 1)}{3K_{sat}} \quad (18)$$

K_{sat} is defined as the ratio of the fundamental components of the air gap voltage for the saturated and unsaturated conditions [14, 28, 29]. Replacing the inverse of (16) in (13), using modified winding function theory, assuming the turn functions have only step variation in the center of the slots and determining the indefinite integrals, exact analytic equations are obtained for various inductances. Then, differentiating the equations versus the rotor position θ_r , exact analytic equations are also obtained for the derivatives of the inductances. The equations are functions of K_{sat} and φ_f , and they are used to include the variable degree of saturation effect within the dynamic model of the SCIM. The proposed equations are given in the appendix. Aforementioned dynamic equations are valid in performance prediction of the SCIM with the rotor faults such as broken rotor bars and end ring. The only modification required is sufficient increase of the resistance of the broken elements such that their currents would diminish.

3. DETERMINING K_{sat} AND φ_f IN FAULTY SCIM

A simple technique to determine φ_f has been offered by [29], but in the faulty SCIM, the air gap flux density distribution disturbs and leads to error in the use of that technique. Also, K_{sat} has been determined using the air gap voltage, which depends on the rotation speed of the air gap flux as well as its amplitude, while the saturation degree depends only on the flux density amplitude [29]. This causes difficulty when applying the model to variable-speed drive systems, as the air gap voltage before saturation is no more a constant, but varies by the reference speed variation. The aim of this section is to resolve these problems.

In simulation of a SCIM using the WFM or SWFM, flux-linkages of all rotor meshes are evaluated at any step. According to (9), these flux linkages have contributions from all the stator phases and rotor meshes. Since any rotor mesh consists of only one turn, these flux-linkages are the total fluxes passing through the meshes. Considering the short air gap length and ignoring some stator flux leakages that return from the air gap and never reach the rotor core, the flux density next to any rotor mesh i within the air gap can be estimated as:

$$B_{ai} = \psi_i / A \quad (19)$$

where A is the area above the mesh in the air gap:

$$A = 2\pi l / R \quad (20)$$

Therefore, an estimation of whole air gap flux density distribution is determined at any simulation step. Then, the space harmonics of the air gap flux density is determined by Fourier series analysis as follows:

$$\begin{aligned} B_{sn} &= \frac{1}{\pi} \int_0^{2\pi} B(\alpha) \sin(nP\alpha) d\alpha \\ &= \frac{1}{\pi} \sum_{i=1}^R B_{ai} \int_{\alpha_i}^{\alpha_{i+1}} \sin(nP\alpha) d\alpha \\ &= -\frac{1}{nP\pi} \sum_{i=1}^R B_{ai} [\cos(nP\alpha_{i+1}) - \cos(nP\alpha_i)] \end{aligned} \quad (21)$$

$$\begin{aligned} B_{cn} &= \frac{1}{\pi} \int_0^{2\pi} B(\alpha) \cos(nP\alpha) d\alpha \\ &= \frac{1}{\pi} \sum_{i=1}^R B_{ai} \int_{\alpha_i}^{\alpha_{i+1}} \cos(nP\alpha) d\alpha \\ &= \frac{1}{nP\pi} \sum_{i=1}^R B_{ai} [\sin(nP\alpha_{i+1}) - \sin(nP\alpha_i)] \end{aligned} \quad (22)$$

Then, the phase angle and amplitude of the space harmonics are calculated as follows:

$$\alpha_n = \tan^{-1} \left(\frac{B_{sn}}{B_{cn}} \right) \quad (23)$$

$$B_n = \sqrt{B_{cn}^2 + B_{sn}^2} \quad (24)$$

The air gap flux density distribution of a SCIM with two broken rotor bars at a simulation step is determined

Figure 1. Estimated air gap flux density (—) and its fundamental space harmonic (---) for a SCIM with two broken rotor bars.

Figure 2. Time variation of φ_f of the SCIM with two broken rotor bars

using (19), and its fundamental space harmonic is calculated using (21)-(24). Figure 1 shows the results where distortion of the flux density due to the fault is obvious. Having the phase angle of the fundamental harmonic, φ_f is estimated as:

$$\varphi_f = \theta_r + \frac{\alpha_1}{P} - \frac{\pi}{2P} \quad (25)$$

Figure 2 shows the variation of φ_f (between $-\pi$ to $+\pi$) versus time obtained during simulation of the SCIM with two broken rotor bars. Constant slope of increase of φ_f indicates constant speed of the air gap flux density, i.e. the synchronous speed. Using the amplitude of the space fundamental harmonic of the air gap flux density, K_{sat} is obtained as follows:

$$K_{sat} = B_1 / B_0 \quad (26)$$

Assuming all the fluxes are concentrated within the teeth, B_0 is related to the knee-point flux density (B_{kp}) of the core material as:

$$B_0 = B_{kp} \frac{w_t}{w} \quad (27)$$

Figure 3 shows the variation of K_{sat} versus the load torque of the healthy and faulty (with two broken rotor bars) SCIMs obtained using simulations. As seen, K_{sat} decreases by increasing load torque. This is because by increasing load torque, stator line current increases, voltage drop across the stator winding resistance and leakage reactance increases, air gap voltage decreases and

Figure 3. Variation of K_{sat} versus load torque in the healthy and faulty (with two broken rotor bars) SCIMs

leads to decrease of the air gap flux and saturation degree. For the load torque above 0.7 pu, decrease of K_{sat} in the faulty SCIM is more than that in the healthy SCIM. This indicates that the fault causes decreasing the amplitude of the space fundamental harmonic of the air gap flux density in the mentioned load torque range. However, at the no-load and light load conditions, K_{sat} curves obtained for healthy and faulty SCIMs are almost coinciding. This is because the rotor bars have small currents at light load conditions, such that the currents of the broken bars diminish. All the simulation results presented in this section are obtained by simulating an 11-kW SCIM by the method introduced in Section 4. More details about the SCIM are given in Section 5.

4. SIMULATION PROCEDURE

Dynamic simulation of SCIM is performed by solving differential Equations (1) - (4) simultaneously. Several methods may be used for this purpose. A rather simple method is described in this section. Assuming simulation time step (Δt) chosen sufficiently small, (1)-(4) can be re-written with good approximation in the form of difference equations as follows:

$$[\psi_s]_i = \{[V_s]_i - [R_s][I_s]_{i-1}\}\Delta t + [\psi_s]_{i-1} \quad (28)$$

$$[\psi_r]_i = -[R_s][I_s]_{i-1}\Delta t + [\psi_r]_{i-1} \quad (29)$$

$$\omega_i = \frac{1}{J}(T_{e,i-1} - T_{L,i})\Delta t + \omega_{i-1} \quad (30)$$

$$\theta_{r,i} = \omega_i\Delta t + \theta_{r,i-1} \quad (31)$$

Also, (8)-(9) can be resolved versus the current vectors as follows:

$$[I_r]_i = ([L_{rr}]_i - [L_{sr}]_i^T [L_{ss}]_i^{-1} [L_{sr}]_i)^{-1} \times ([\psi_r]_i - [L_{sr}]_i^T [L_{ss}]_i^{-1} [\psi_s]_i) \quad (32)$$

$$[I_s]_i = [L_{ss}]_i^{-1} [\psi_s]_i - [L_{ss}]_i^{-1} [L_{sr}]_i [I_r]_i \quad (33)$$

The simulation procedure proceeds as indicated in the flowchart of Figure 4. As seen, the simulation procedure starts with the initialization stage. Then, it enters the simulation steps loop, where various parameters and variables of the SCIM are calculated at every step using given equations. The loop repeats until the end of simulation time. The stated simulation method is similar to the numerical solution of the state equations and can be performed using general purpose software codes such as MATLAB.

5. EXPERIMENTAL TEST RIG

The proposed test rig consists of an 11-kW, 380-V, 50-Hz, 4-poles, Δ -connected industrial SCIM mechanically coupled to a DC generator, while a variable resistor bank is connected to the terminals of the generator. The load of the generator, and consequently the SCIM is adjusted by varying the resistance of the resistor bank. A PC equipped with a data acquisition (DAQ) card type PCI-1710HG is used for sampling the required electrical data at certain adjustable frequency [31]. Additional rotor with broken bars are provided to do experiments under the rotor broken bar conditions. Required number of adjacent bars was broken by drilling holes in them. Figure 5 shows a photograph of the test rig.

6. COMPARISON OF SIMULATION AND EXPERIMENTAL RESULTS

To validate the simulation results of the proposed SWFM, they are compared with the corresponding experimental results. In addition, simulation results from SWFM are compared with those from WFM to verify magnetic saturation impacts. Figure 6 shows the no-load phase current of the healthy SCIM. As seen, the current is rather sinusoidal with half-nominal stator voltage, but it is disturbed with nominal stator voltage. This is due to some degree of saturation occurring under nominal voltage.

To verify this, magnetization curve of the motor has been determined by experiment as well as simulation and is shown in Figure 7. As seen, the nominal voltage of the motor is above knee of the magnetization curve.

In both Figures 6 and 7, simulation and experimental results agree well and this implies the high accuracy of the developed SWFM.

Representing a broken bar with zero current as the superposition of a healthy bar and a current source injecting a current in the bar of opposite value as the current flowing in the healthy bar, and using an approach based on the rotating magnetic fields, it could be realized that the bar breakage induces currents at frequencies $(1 \pm 2s)f$ in the stator windings, where f is the supply fundamental frequency [4, 11, 12, 32].

Figure 4. The simulation procedure flowchart

Figure 5. Photograph of the test rig

Figure 6. No-load phase current of healthy SCIM with nominal (—) and half-nominal (---) stator voltages: a) simulation using the SWFM, b) experimental.

Figure 7. Stator line voltage versus its no-load current (magnetization curve) obtained by experiment and simulation using the SWFM for the healthy SCIM and SCIM with two broken bars

These frequency components (sidebands) are the main signatures of the broken rotor bars fault in the stator currents, which are generally used as indexes for the fault diagnosis. Normalized frequency spectra of the stator line current are shown in Figure 8 for the healthy SCIM and the SCIM with one and two broken bars under half rated load. Comparison can be made between the results obtained through simulation using the WFM and the SWFM as well as the results obtained from experiments. As seen, the sidebands are clear in the spectra and their amplitudes are amplified due to the fault. Also, the amplitudes in the SWFM results are much closer to those in the experimental results. In the SWFM and the experimental results, non-uniform effect of the magnetic saturation is the cause for the presence of the sidebands in the healthy SCIM and for the increase of their amplitudes in the faulty SCIM. This has been also reported in [4]. Therefore, the proposed SWFM provides more precise results and it is more reasonable to analyze the SCIM with broken rotor bars than the WFM. The broken rotor bar fault intensifies the space harmonics of the air gap flux density. Figure 9 shows the variation of the amplitude of the 3rd space harmonic of the air gap flux density obtained by the SWFM as well as the WFM.

Figure 8. Normalized frequency spectra of the stator line current obtained through simulation using the SWFM (a, b, c), the WFM (d, e, f) and the experiments (g, h, i) for the healthy SCIM (a, d, g), for the SCIM with one broken rotor bar (b, e, h) and for the SCIM with two broken rotor bars (c, f, i) under half rated load.

Figure 9. Amplitude variation of the 3rd space harmonic of the air gap flux density obtained by the SWFM (a,c,e) and by the WFM (b,d,f) for: a,b) healthy SCIM, c,d) SCIM with 1 broken bar, and e,f) SCIM with two Broken bars.

Figure 10. Estimated rotor teeth flux densities in healthy (---) and 1 broken bar (—) SCIMs obtained using: a) the SWFM and b) the WFM.

It must be noticed that the traces in the charts in this figure are not synchronized, since they are obtained from different simulation processes on the SCIM. As seen, the rotor bar breakage increases the fluctuation amplitude of the 3rd space harmonic of the air gap flux density (especially with two broken bars). Also, the clear effect of saturation on the behavior of this harmonic amplitude in the healthy and faulty SCIMs is noticeable. Due to saturation, normal tedious variation of the harmonic amplitude disturbs and its maximum value increases. The SWFM results in Figure 9 are qualitatively in agreement with the corresponding experimental result given in reference [32].

Figure 10 shows the rotor teeth flux densities determined by using rotor meshes flux linkages and by assuming the total flux passing through any rotor mesh concentrates in the relevant rotor tooth uniformly. As seen, a broken rotor bar reduces the flux of an adjacent tooth and increases that of other adjacent tooth. This is more significant in the SWFM results and leads to a higher local saturation in the latter tooth. The SWFM results are in more agreement with the similar finite elements results given in [12].

7. CONCLUSION

The flux linkages of the rotor meshes calculated in every simulation step by the winding function approach were used to estimate the air gap flux density distribution. Then, space harmonic components of the air gap flux density were determined using Fourier series analysis. The phase angle of the space fundamental harmonic was utilized to locate the air gap flux density during simulation of the faulty SCIMs. The amplitude of this fundamental harmonic is applicable to evaluate the saturation factor more reasonably. A comparison between the simulation and experimental results verified the better accuracy of the developed

saturable model, which means that more precise fault diagnosis techniques can be designed by using the proposed saturable model. The saturation impacts on various quantities of the SCIM, such as the stator line current spectrum and the air gap flux density distribution can be analyzed by comparing the results obtained from saturable and non-saturable models.

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APPENDICES

Analytic equation for the stator self/mutual inductances is obtained as follows:

$$L_{xy} = \mu_0 r l \sum_{i=1}^m n_x(\varphi_{ii}) [n_y(\varphi_{ii}) - f_s(\varphi_f, K_{sat})] \times [f(\varphi_{i+1}, \varphi_f, K_{sat}) - f(\varphi_i, \varphi_f, K_{sat})] \quad (A1)$$

where x and y represent the stator phases, m is the number of the stator slots, φ_i the angle of center of the stator slot i , φ_{ii} the angle of center of the stator tooth after its slot i and functions $f(\cdot)$ and $f_s(\cdot)$ are:

$$f(\varphi, \varphi_f, K_{sat}) = \int \frac{d\varphi}{g_s(\varphi, \varphi_f, K_{sat})} = \frac{1}{2p g' \sqrt{1-\rho^2}} \cos^{-1} \left(\frac{\cos(2p(\varphi - \varphi_f)) - \rho}{1 - \rho \cos(2p(\varphi - \varphi_f))} \right) \quad (A2)$$

$$f_s(\varphi_f, K_{sat}) = \frac{g' \sqrt{1-(\rho)^2}}{2\pi} \sum_{i=1}^m n_y(\varphi_{ii}) \times [f(\varphi_{i+1}, \varphi_f, K_{sat}) - f(\varphi_i, \varphi_f, K_{sat})] \quad (A3)$$

The stator inductances are constants, thus their derivatives versus the rotor position are zero. Analytic equation for the rotor self/mutual inductances is obtained as follows:

$$L_{uv} = \mu_0 r l [c - f_r(\alpha_f, K_{sat})] [f(\alpha_{u+1}, \alpha_f, K_{sat}) - f(\alpha_u, \alpha_f, K_{sat})] \quad (A4)$$

where u and v represent the rotor meshes 1 to R , α_f is φ_f in the rotor frame of reference ($\alpha_f = \varphi_f - \theta_r$), α_u is the angle of center of bar number u in the rotor frame, c is equal to 1 for $u = v$ and equal to 0 otherwise, and function f_r is:

$$f_r(\alpha_f, K_{sat}) = \frac{g' \sqrt{1-(\rho)^2}}{2\pi} [f(\alpha_{v+1}, \alpha_f, K_{sat}) - f(\alpha_v, \alpha_f, K_{sat})] \quad (A5)$$

As α_f depends on the rotor position (θ_r), (A4) and (A5) are so dependent. Considering $\partial L_{xy} / \partial \theta_r = -\partial L_{xy} / \partial \alpha_f$ the

equation for the derivatives of the rotor inductances is obtained as follows:

$$\frac{\partial L_{uv}}{\partial \theta} = -\mu_o r l [c - f_r(\alpha_f, K_{sat})] \left[\frac{\partial f(\alpha_{u+1}, \alpha_f, K_{sat})}{\partial \alpha_f} - \frac{\partial f(\alpha_u, \alpha_f, K_{sat})}{\partial \alpha_f} \right] + \mu_o r l \frac{\partial f_r(\alpha_f, K_{sat})}{\partial \alpha_f} [f(\alpha_{u+1}, \alpha_f, K_{sat}) - f(\alpha_u, \alpha_f, K_{sat})] \quad (A6)$$

where:

$$\frac{\partial f_r(\alpha_f, K_{sat})}{\partial \alpha_f} = \frac{g' \sqrt{1-(\rho)^2}}{2\pi} \left[\frac{\partial f(\alpha_{y+1}, \alpha_f, K_{sat})}{\partial \alpha_f} - \frac{\partial f(\alpha_y, \alpha_f, K_{sat})}{\partial \alpha_f} \right] \quad (A7)$$

$$\frac{\partial f(\alpha_i, \alpha_f, K_{sat})}{\partial \alpha_f} = \frac{-1}{g' [1 - \rho^s \cos(2p(\alpha_i - \alpha_f))]} ; \quad (A8)$$

$$\alpha_i = \alpha_{u+1}, \alpha_u, \alpha_{v+1}, \alpha_v$$

The mutual inductances between the rotor meshes and the stator phases are obtained as follows:

$$L_{ux} = \mu_o r l \sum_{i=k_1}^{k_2+1} [n_y(\varphi_{ti-1}) - f_s(\varphi_f, K_{sat})] \times [f(\varphi_i, \varphi_f, K_{sat}) - f(\varphi_{i-1}, \varphi_f, K_{sat})] \quad (A9)$$

where u and x represent the rotor meshes and the stator phases respectively, φ_{k1-l} and φ_{k2+l} are the angles of the two bars of mesh u in the stator reference, k_1 to k_2 are the stator slots between φ_{k1-l} and φ_{k2+l} (e.g. φ_{k1} is the angle of the stator slot k_1). Now φ_{k1-l} and φ_{k2+l} depend on θ_r such that their derivatives versus θ_r are equal to 1, while other parameters in (A9) are independent of θ_r . Using these facts, and some differentiation leads to:

$$\frac{\partial L_{ux}}{\partial \theta} = \mu_o r l \left(\begin{aligned} & - \frac{[n_x(\varphi_{tk1-1}) - f_s(\varphi_f, K_{sat})]}{g' [1 - \rho \cos(2p(\varphi_{k1-1} - \varphi_f))]} \\ & + \frac{[n_x(\varphi_{tk2}) - f_s(\varphi_f, K_{sat})]}{g' [1 - \rho \cos(2p(\varphi_{k2+1} - \varphi_f))]} \end{aligned} \right) \quad (A10)$$

Exact Modeling and Simulation of Saturated Induction Motors with Broken Rotor Bars Fault using Winding Function Approach

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چکیده

روش تابع سیم پیچ یک روش شبیه سازی و مدل سازی دقیق و نسبتاً ساده برای تحلیل عملکرد موتورهای القایی قفس سنجابی معیوب ارائه می کند. این روش برای شناسایی لحظه ای خطا قابل اعمال است. در این مقاله، روش تابع سیم پیچ با اعمال درجات متغیر اشباع مغناطیسی با به کار بردن یک تابع فاصله هوایی مناسب و نیز روشی جدید برای تخمین ضریب اشباع مورد نیاز و موقعیت زاویه ای چگالی شار فاصله هوایی ارائه شده است. در نتیجه، مدل تابع سیم پیچ اشباع پذیر برای تحلیل موتور القایی قفس سنجابی دارای عیب میله های شکسته شده روتور و همچنین برای شناسایی اثر اشباع روی شاخص های عیب مربوطه به کار رفته است. مقایسه نتایج شبیه سازی با نتایج آزمایشی متناظر نشان می دهد که مدل تابع سیم پیچ اشباع پذیر دارای دقت زیادی است. این بدان معناست که با استفاده از این مدل اشباع پذیر می توان روش های تشخیص عیب دقیق تری طراحی نمود.

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